| Not One of Them |  |
| :---: | :---: |
| Costly Binary Search |  |
| Log Drivin' Hirin' | Topic-related <br> tasks |
| City Hall |  |
| Harbingers | Still DP |
| Camel and Oases |  |
| Shores | "Stolen" from a <br> contest, sorted by <br> (expected) <br> hardest to easiest |
| Sending Blessings |  |
| Go To Goal |  |
| Healthy Lifestyle |  |
| Frequent Alphabet |  |


| I | Not One of Them |  |
| :---: | :---: | :---: |
| C | Costly Binary Search | Topic-related <br> tasks |
| B | Log Drivin' Hirin' |  |
| D | City Hall |  |
| K | Carbingers | Still DP |

## as promised, one more task that has not been discussed yesterday

IOI 2014 Holiday (reduced)
given $N$ cities in a line. City i has value $A[i]$. You start at city 0 . In one day, you can either move to neighbouring city or take the value (at most once) of the current city.

For each $d=0 . .2 \mathrm{~N}$, determine the maximum total value you can get if you have d days

$$
1 \leq N \leq 100 k
$$

find the value of single d can be done in $\mathrm{O}(\mathrm{N} \lg \mathrm{N})$ by iterating which rightmost city to be visited.
let opt(d) = the farthest city you visit when you have d days in the optimal solution.
we have opt(d) $\leq \operatorname{opt}(d+1)$

## Graph Connectivity

Jonathan Irvin Gunawan

$$
\begin{aligned}
& \text { let's practice some } \\
& \text { tasks }
\end{aligned}
$$

## IOI 2015 Practice Graph

given a graph and two nodes A, B. determine how many vertices which, if removed, disconnects $A$ and $B$

$$
\begin{aligned}
& 1 \leq N \leq 100.000 \\
& 0 \leq M \leq 200.000
\end{aligned}
$$

## run DFS tree with root $=A$

the possible candidate vertices are vertices in the path from $A$ to $B$

## node $u$ is an answer if

## let's say $v$ is a child of $u$ where $v=$ ancestor(B). dfs_low[v] $\geq$ dfs_num[u]

## more

https://www.hackerearth.com/practice/
algorithms/graphs/strongly-connected-components/practice-problems/algorithm/ a-walk-to-remember-qualifier2/
given a directed graph, for each node, determine whether there is a cycle staring from the node

$$
\begin{aligned}
& 1 \leq N \leq 100.000 \\
& 1 \leq M \leq 200.000
\end{aligned}
$$

## just check for each node whether that node is alone in the SCC

## one more

http://acm.timus.ru/forum/thread.aspx? $i d=22089 \& u p d=633721365703625916$
given a directed graph, determine which nodes can go to ALL other nodes.

$$
\begin{aligned}
& 1 \leq N \leq 100.000 \\
& 0 \leq M \leq 200.000
\end{aligned}
$$

so the observation is, if $a$ and $b$ is in one SCC, then the set of vertices that can be visited by a and $b$ is exactly the same.
therefore, run SCC, group nodes in one SCC to be one node.

There is an edge from SCC node $a$ to $b<=>$ there is an edge from node $u$ to $v$ where $u$ is in $a$ and $v$ is in $b$
this technique is quite common. let's name it SCC graph
now we got a DAG (otherwise SCC is not optimal)
then, just choose a candidate node (vertex without an indegree), then check whether that node can visit all other nodes

## last

ICPC Jakarta Regional 2012 Unique Path
given a graph, find the number of pair of nodes with unique path

$$
\begin{aligned}
& 2 \leq N \leq 10 k \\
& 1 \leq M \leq 100 k
\end{aligned}
$$



Q\&A?

